

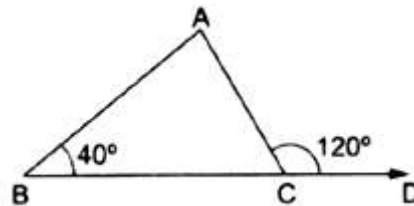
# MATHS SAMPLE PAPER

## PART-A

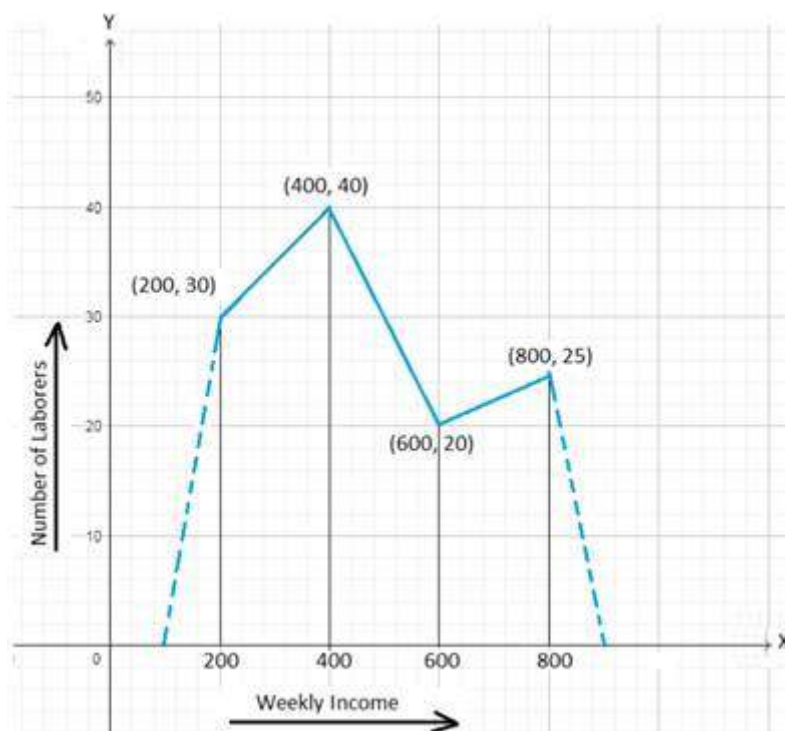
### Section-I

Section I has 16 questions of 1 mark each.

1. The complement of  $72^{\circ}40'$  is \_\_\_\_\_.
2. In  $\triangle ABC$ , side BC is produced to D. If  $\angle ABC = 40^{\circ}$  and  $\angle ACD = 120^{\circ}$ , then find  $\angle A$ .



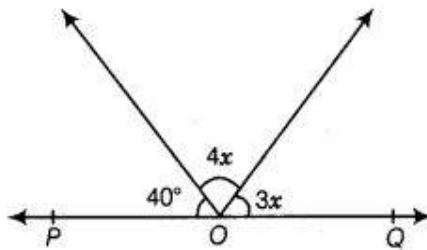
3. Three angles of a quadrilateral measure  $56^\circ$ ,  $115^\circ$  and  $84^\circ$ . Find the measure of the fourth angle.
4. A chord of length 16 cm is drawn in a circle of radius 10 cm. Find the distance of the chord from the center of the circle.
5. The base of an isosceles triangle is 16 cm and its area is  $48\text{cm}^2$ . The perimeter of the triangle is \_\_\_\_\_.
6. Find the length of the longest pole that can be put in a room of dimensions  $(10\text{ m} \times 10\text{ m} \times 5\text{ m})$ .
7. The following frequency polygon displays the weekly incomes (in Rs) of labourers of a factory.



How many labourers have a weekly income of Rs 400?

8. In 50 tosses of a coin, tail appears 32 times. If a coin is tossed at random, what is the probability of getting a head?

9. Abscissa of all points on the Y-axis is \_\_\_\_\_.
10.  $\sqrt{2}$  is a polynomial of degree \_\_\_\_\_.
11. If (2, 0) is a solution of the linear equation  $2x + 3y = k$ , then the value of  $k$  is \_\_\_\_\_.
12. In  $\triangle ABC$ ,  $AB = AC$  and  $\angle B = 50^\circ$ . Then  $\angle A$  is equal to \_\_\_\_\_.
13. If  $p(x) = x^2 - 2\sqrt{2}x + 1$ , then find the value of  $p(2\sqrt{2})$ .
14. In the given fig, POQ is a line. The value of  $x$  is:



15. An isosceles right triangle has area  $8 \text{ cm}^2$ , what will be the length of its hypotenuse?
16. What will be the rationalising factor of  $\frac{1}{\sqrt{9}-\sqrt{8}}$ ?

## Section II

**Case-study based questions are compulsory. Attempt any four sub parts of each question. Each subpart carries 1 mark**

17. Case study based-1: The Pythagoreans in Greece, followers of the famous mathematician and philosopher Pythagoras, were the first to discover the numbers which were not rationals, around 400 BC. These numbers are called irrational numbers (irrationals), because they cannot be written in the form of a ratio of integers. There are many myths surrounding the discovery of irrational numbers by the Pythagorean, Hippacus of Croton. In all the myths, Hippacus has an unfortunate end, either for discovering that 2 is irrational or for disclosing the secret about 2 to people outside the secret Pythagorean sect!

(a) Which of the following numbers is not rational?

- (i)  $\frac{3}{2}$  (ii)  $\frac{\sqrt{3}}{7}$  (iii) 0.54 (iv)  $5.\overline{23}$ .
- (b) Which of the following numbers is not irrational?  
 (i) 0.1232453467896548...  
 (ii)  $\sqrt{7}$   
 (iii)  $\pi$   
 (iv)  $\frac{22}{7}$
- (c) The product of a rational and an irrational number is always  
 (i) Rational (ii) irrational (iii) integer (iv) non real number
- (d) An irrational number between 2 and 2.5 is  
 (i)  $\sqrt{11}$  (ii)  $\sqrt{5}$  (iii)  $\sqrt{22.5}$  (iv)  $\sqrt{12.5}$
- (e) The value of  $0.\overline{23} + 0.\overline{22}$  is  
 (i)  $0.\overline{45}$   
 (ii)  $0.\overline{43}$   
 (iii)  $0.4\overline{5}$   
 (iv) 0.45

**18.** Case study based – 2: Consider a square of side 3 units. What is its perimeter? You know that the perimeter of a square is the sum of the lengths of its four sides. Here, each side is 3 units. So, its perimeter is  $4 \times 3$ , i.e., 12 units. What will be the perimeter if each side of the square is 10 units? The perimeter is  $4 \times 10$ , i.e., 40 units. In case the length of each side is  $x$  units, the perimeter is given by  $4x$  units. So, as the length of the side varies, the perimeter varies. Can you find the area of the square PQRS? It is  $x \times x = x^2$  square units.  $x^2$  is an algebraic expression. You are also familiar with other algebraic expressions like  $2x$ ,  $x^2 + 2x$ ,  $x^3 - x^2 + 4x + 7$ . Note that, all the algebraic expressions we have considered so far have only whole numbers as the exponents of the variable. Expressions of this form are called polynomials in one variable. In the examples above, the variable is  $x$ . For instance,  $x^3 - x^2 + 4x + 7$  is a polynomial in  $x$ . Similarly,  $3y^2 + 5y$  is a polynomial in the variable  $y$  and  $t^2 + 4$  is a polynomial in the variable  $t$ .

- (a) Degree of the polynomial  $p(x) = (x + 1)(x - 1)$  is  
 (i) 2 (ii) 1 (iii) 0 (iv) None of these
- (b) The zero of the polynomial  $p(x) = 2x + 5$  is  
 (i)  $-\frac{2}{5}$  (ii)  $-\frac{5}{2}$  (iii)  $\frac{2}{5}$  (iv)  $\frac{5}{2}$
- (c) Which of the following is a polynomial?  
 (i)  $p(x) = 3x^2 + \sqrt{x}$   
 (ii)  $p(x) = x + \frac{2}{x}$   
 (iii)  $p(x) = 7x^2 - 3x^{\frac{-3}{2}} + 11$



$$(iv) \quad p(x) = \frac{7x^{\frac{3}{2}}}{\sqrt{x}}$$

- (d) The coefficient of  $x$  in the expansion of  $(x + 3)^3$  is  
 (i) 9 (ii) 18 (iii) 27 (iv) None of these
- (e) If  $x - 2$  is a factor of  $x^2 + 3ax - 2a$ , then  $a$  is  
 (i) 2 (ii) -2 (iii) 1 (iv) -1

**19.** Case study based -3: René Descartes, the great French mathematician of the seventeenth century, liked to lie in bed and think! One day, when resting in bed, he solved the problem of describing the position of a point in a plane. His method was a development of the older idea of latitude and longitude. In honour of Descartes, the system used for describing the position of a point in a plane is also known as the Cartesian system.

- (a) The coordinate of a point in the third quadrant is of the form  
 (i) (+, +) (ii) (-, +) (iii) (+, -) (iv) (-, -)
- (b) The point of intersection of the axes is called the  
 (i) Ordinate (ii) Abscissa (iii) Origin (iv) None of these
- (c) The point(-5, 8) lies in the \_\_\_\_\_ Quadrant  
 (i) I (ii) II (iii) III (iv) IV
- (d) Ordinate of all points on the  $x$ -axis is  
 (i) 3 (ii) 4 (iii) 2 (iv) 0
- (e) If  $x \neq y$ , then the point  $(x, y)$  in the cartesian plane is  
 (i) Same as  $(y, x)$   
 (ii) Different from  $(y, x)$   
 (iii) Depends on the values of  $x$  and  $y$   
 (iv) None of these

**20.** Case study based - 4: In countries like USA and Canada, temperature is measured in Fahrenheit, whereas in countries like India, it is measured in Celsius. Here is a linear equation that converts Fahrenheit to Celsius:

$$F = \left(\frac{9}{5}\right)C + 32$$

Answer the questions that follow.

- (a) If the temperature is  $30^\circ\text{C}$ , what is the temperature in Fahrenheit?  
 (i)  $96^\circ\text{F}$  (ii)  $86^\circ\text{F}$  (iii)  $108^\circ\text{F}$  (iv)  $37^\circ\text{F}$



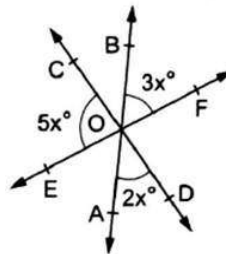
- (b) If the temperature is  $95^{\circ}\text{F}$ , what is the temperature in Celsius?  
 (i)  $37.5^{\circ}\text{C}$  (ii)  $36^{\circ}\text{C}$  (iii)  $35^{\circ}\text{C}$  (iv)  $34.7^{\circ}\text{C}$
- (c) If the temperature is  $0^{\circ}\text{C}$ , what is the temperature in Fahrenheit?  
 (i)  $29^{\circ}\text{F}$  (ii)  $31^{\circ}\text{F}$  (iii)  $32^{\circ}\text{F}$  (iv)  $-40^{\circ}\text{F}$
- (d) If the temperature is  $0^{\circ}\text{F}$ , what is the temperature in Celsius?  
 (i)  $-17.77^{\circ}\text{C}$  (ii)  $31.65^{\circ}\text{C}$  (iii)  $101^{\circ}\text{C}$  (iv) None of these
- (e) Find the temperature which is numerically the same in both Fahrenheit and Celsius.  
 (i) 40  
 (ii) 0  
 (iii) -40  
 (iv) 273

## PART-B

### Section III

**21.** Evaluate: (i)  $(81)^{-1/4}$  (ii)  $\left(\frac{1}{3^4}\right)^{\frac{1}{2}}$

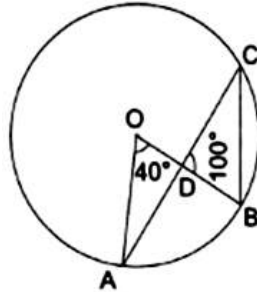
**22.** In the adjoining, there coplanar lines AB, CD and EF intersect at a point O. Find the value of x. Hence, find  $\angle AOD$ ,  $\angle COE$  and  $\angle AOE$ .



**23.** If the base of an isosceles triangle is produced on both sides, prove that the exterior angles so formed are equal to each other.



**24.** In the adjoining figure,  $O$  is the center of a circle,  $\angle AOB = 40^\circ$  and  $\angle BDC = 100^\circ$ , find  $\angle OBC$ .



**25.** The sides of triangle are in the ratio 5 : 12 : 13 and its perimeter is 150m. Find the area of triangle.

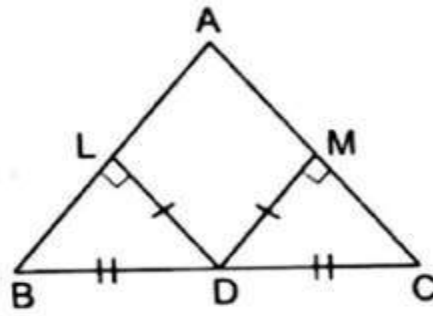
**26.** In a survey of 200 ladies, it was found that 142 like coffee, while 58 dislike it.

Find the probability that a lady chosen at random  
(i) likes coffee, (ii) dislikes coffee.

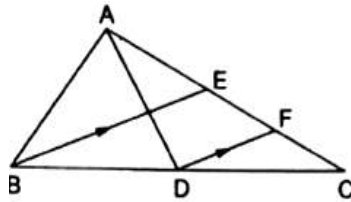
### Section IV

**27.** The Polynomial  $f(x) = x^4 - 2x^3 + 3x^2 - ax + b$  when divided by  $(x-1)$  and  $(x+1)$  leaves the remainders 5 and 19 respectively. Find the values of  $a$  and  $b$ . Hence, find the remainder when  $f(x)$  is divided by  $(x-2)$ .

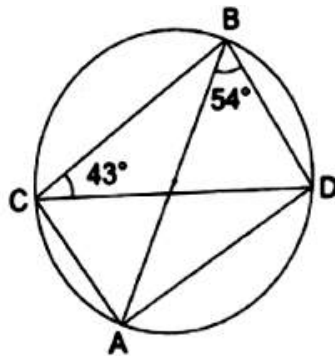
**28.** In  $\triangle ABC$ ,  $D$  is the midpoint of  $BC$ . If  $DL \perp AB$  and  $DM \perp AC$  such that  $DL=DM$ , prove that  $AB=AC$ .



**29.** In the adjoining figure,  $AD$  and  $BE$  are the medians of  $\triangle ABC$  and  $DF \parallel BE$ . Show that  $CF = \frac{1}{4}AC$ .



**30.** In the given figure,  $\angle ABD = 54^\circ$  and  $\angle BCD = 43^\circ$ , calculate  
 (i)  $\angle ACD$  (ii)  $\angle BAD$  (iii)  $\angle BDA$



**31.** The base of an isosceles triangle measures 80cm and its area is  $360\text{cm}^2$ . Find the perimeter of the triangle.



**32.** A wall 15 m long, 30 cm wide and 4 m high is made of bricks, each measuring  $(22 \text{ cm} \times 12.5 \text{ cm} \times 7.5 \text{ cm})$ . If  $\frac{1}{12}$  of the total volume of the wall consists of mortar, how many bricks are there in the wall?

**33.** Following are the ages (in years) of 360 patients, getting medical treatment in a hospital:

Age (in years)	10-20	20-30	30-40	40-50	50-60	60-70
Number of patients	90	50	60	80	50	30

One of the patients is selected at random. Find the probability that his age is

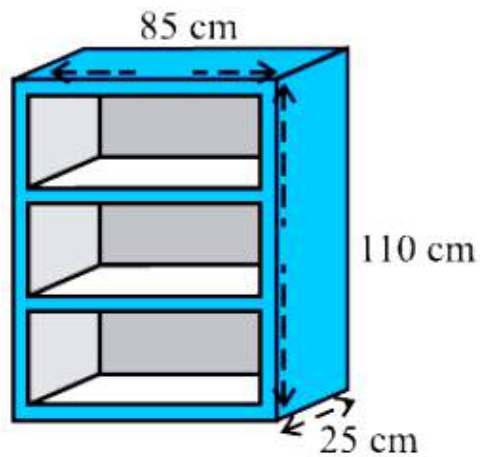
- 30 Year or more but less than 40 years.
- 50 year or more but less than 70 years
- Less than 10 years.

### Section V

**34.** Construct a triangle PQR in which  $QR = 6\text{cm}$ ,  $\angle Q = 60^\circ$  and  $PR - PQ = 2\text{cm}$ . Mention the steps of construction.

**35.** A wooden bookshelf has external dimensions as follows: Height = 110 cm, Depth = 25 cm, Breadth = 85 cm. The thickness of the plank is 5 cm everywhere. The external faces are to be polished and the inner faces are to be painted. If the rate of polishing is 20 paise per  $\text{cm}^2$  and the rate of painting is 10 paise per  $\text{cm}^2$ , find the total expenses required for polishing and painting the surface of the bookshelf.





**36.** The length of 40 leaves of a plant are measured correct to one millimetre, and the obtained data is represented in the following table:

Length (in mm)	Number of leaves
118 - 126	3
127 - 135	5
136 - 144	9
145 - 153	12
154 - 162	5
163 - 171	4
172 - 180	2

- (i) Draw a histogram to represent the given data.  
(ii) Is it correct to conclude that the maximum number of leaves are 153 mm long? Why?

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## Hints and Solutions

### PART – A

#### Section - I

1.  $17^{\circ}20'$
2.  $80^{\circ}$
3.  $105^{\circ}$
4. 6 cm
5. 36 cm
6. 15 m
7. 40
8.  $9/25$
9. 0
10. 0
11. 4
12.  $80^{\circ}$
13. 1
14.  $20^{\circ}$
15.  $4\sqrt{2}$  cm
16.  $\sqrt{9} + \sqrt{8}$

#### Section -II

17. (a) (ii)  $\sqrt{3}/7$   
(b) (iv)  $22/7$   
(c) (ii) Irrational  
(d) (ii)  $\sqrt{5}$   
(e) (i)  $0.\overline{45}$
18. (a) (i) 2  
(b) (ii)  $-5/2$



(c) (iv)  $p(x) = \frac{7x^{\frac{3}{2}}}{\sqrt{x}}$

(d) (iii) 27

(e) (iv) -1

19. (a) (iv) (-, -)

(b) (iii) Origin

(c) (ii) II

(d) (iv) 0

(e) (ii) Different from (y, x)

20. (a) (ii) 86°F

(b) (iii) 35°C

(c) (iii) 32°F

(d) (i) -17.77°C

(e) (iii) -40

## PART – B

### Section – III

21. (i)  $(81)^{-\frac{1}{4}} = (3^4)^{-\frac{1}{4}} = (3)^{4 \times -\frac{1}{4}} = 3^{-1} = \frac{1}{3}$ .

(ii)  $\left(\frac{1}{3^4}\right)^{\frac{1}{2}} = (3^{-4})^{\frac{1}{2}} = (3)^{-4 \times \frac{1}{2}} = 3^{-2} = \frac{1}{9}$

22.  $\angle AOD + \angle DOF + \angle BOF + \angle BOC + \angle COE + \angle AOE = 360^\circ$

$\Rightarrow 2x + 5x + 3x + 2x + 5x + 3x = 360^\circ$

$\Rightarrow 20x = 360^\circ$

$\Rightarrow x = 18^\circ$

$\angle AOD = 2x = 2 \times 18^\circ = 36^\circ$

$\angle AOE = 3x = 3 \times 18^\circ = 54^\circ$

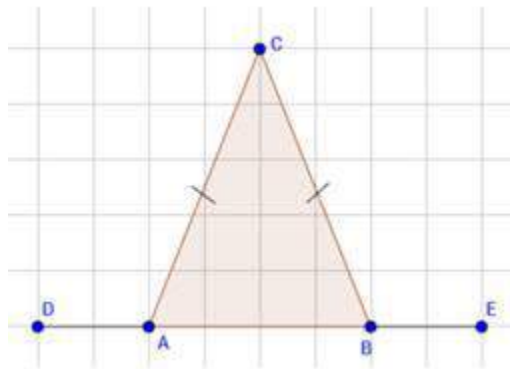
$\angle COE = 5x = 5 \times 18^\circ = 90^\circ$



**23.** Given:  $\triangle ABC$  is isosceles triangle.

To prove:  $\angle CAD = \angle CBE$

Let  $\triangle ABC$  be our isosceles triangle as shown in the figure.



We know that base angles of the isosceles triangle are equal.

Here,  $\angle CAB = \angle CBA \dots(1)$

Also here,  $\angle CAD$  and  $\angle CBE$  are exterior angles of the triangle.

So, we know that,

$\angle CAB + \angle CAD = 180^\circ \dots$  exterior angle theorem

And  $\angle CBA + \angle CBE = 180^\circ \dots$  exterior angle theorem

So from (1) and above statement, we conclude that,

$\angle CAB + \angle CAD = 180^\circ$

And  $\angle CAB + \angle CBE = 180^\circ$

Which implies that,

$\angle CAD = 180^\circ - \angle CAB$

And  $\angle CBE = 180^\circ - \angle CAB$

Hence we say that  $\angle CAD = \angle CBE$

$\therefore$  For the isosceles triangle, the exterior angles so formed are equal to each other.

**24.**  $\angle DCB = (1/2) \angle AOB$  [ $\angle DCB = \angle ACB$ ]

$$\Rightarrow \angle DCB = (1/2) 40^\circ$$

$$\Rightarrow \angle DCB = 20^\circ$$

In triangle BCD,

$$\angle BDC + \angle DCB + \angle DBC = 180^\circ \text{ [Sum of angles of triangle]}$$

$$\Rightarrow 100^\circ + 20^\circ + \angle OBC = 180^\circ$$

$$\Rightarrow 120^\circ + \angle DBC = 180^\circ$$

$$\Rightarrow \angle DBC = 60^\circ$$

$$\therefore \angle OBC = \angle DBC = 60^\circ$$

**25.** Let the sides of the given triangle be  $5x$ ,  $12x$  and  $13x$

Given,

$$\text{Perimeter of the triangle} = 150\text{m}$$

$$\text{Perimeter of the triangle} = (5x + 12x + 13x)$$

$$150 = 30x$$

Therefore,

$$x = \frac{150}{30} = 5\text{ m}$$

Thus,

Sides of the triangle are:

$$5x = 5 \times 5 = 25\text{ m}$$

$$12x = 12 \times 5 = 60\text{ m}$$

$$13x = 13 \times 5 = 65\text{ m}$$

Let,

$$a = 25\text{ m}, b = 60\text{ m and } c = 65\text{ m}$$

Therefore,

$$s = \frac{1}{2} (a + b + c)$$

$$= \frac{1}{2} (25 + 60 + 65)$$



$$= \frac{1}{2} (150)$$

$$= 75 \text{ m}$$

We know that,

$$\text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{75(75-25)(75-60)(75-65)}$$

$$= \sqrt{75 \times 50 \times 15 \times 10}$$

$$= \sqrt{25 \times 3 \times 25 \times 2 \times 5 \times 3 \times 5 \times 2}$$

$$= \sqrt{25 \times 25 \times 5 \times 5 \times 3 \times 3 \times 2 \times 2}$$

$$= 25 \times 5 \times 3 \times 2$$

$$= 750 \text{ sq m}$$

Hence, area of triangle is 750 sq m.

**26.** Total number of ladies: 200

Number of ladies who like coffee: 142

Number of ladies who dislike coffee: 58

$$\text{Probability } P(E) = \frac{\text{Number of favorable outcomes}}{\text{Total number of outcomes}}$$

(i). Let  $p(\text{Coffee})$  be probability of ladies who like coffee

$$P(\text{Coffee}) = \frac{\text{Number of ladies who like coffee}}{\text{Total number ladies}}$$

$$P(\text{Coffee}) = \frac{142}{200} = 0.71$$

(ii). Let  $p(\text{No Coffee})$  be probability of ladies who dislikes coffee

$$P(\text{No Coffee}) = \frac{\text{Number of ladies who dislike coffee}}{\text{Total number of ladies}}$$

$$P(\text{No Coffee}) = \frac{58}{200} = 0.29$$



## Section – IV

**27.** Let  $f(x) = x^4 - 2x^3 + 3x^2 - ax + b$

Now,

$$f(1) = 1^4 - 2(1)^3 + 3(1)^2 - a(1) + b$$

$$5 = 1 - 2 + 3 - a + b$$

$$3 = -a + b \text{ (i)}$$

And,

$$f(-1) = (-1)^4 - 2(-1)^3 + 3(-1)^2 - a(-1) + b$$

$$19 = 1 + 2 + 3 + a + b$$

$$13 = a + b \text{ (ii)}$$

Now,

Adding (i) and (ii),

$$8 + 2b = 24$$

$$2b = 16$$

$$b = 8$$

Now,

Using the value of  $b$  in (i)

$$3 = -a + 8$$

$$a = 5$$

Hence,

$$a = 5 \text{ and } b = 8$$

Hence,

$$f(x) = x^4 - 2(x)^3 + 3(x)^2 - a(x) + b$$

$$= x^4 - 2x^3 + 3x^2 - 5x + 8$$

$$f(2) = (2)^4 - 2(2)^3 + 3(2)^2 - 5(2) + 8$$

$$= 16 - 16 + 12 - 10 + 8$$

$$= 20 - 10$$

$$= 10$$

Therefore, remainder is 10



**28.** Given:  $BD = DC$  and  $DL \perp AB$  and  $DM \perp AC$  such that  $DL = DM$

To prove:  $AB = AC$

Proof:

In right angled triangles  $\triangle BLD$  and  $\triangle CMD$ ,

$$\angle BLD = \angle CMD = 90^\circ$$

$$BD = CD \dots \text{given}$$

$$DL = DM \dots \text{given}$$

Thus by right angled hypotenuse side property of congruence,

$$\triangle BLD \cong \triangle CMD$$

Hence, we know that, corresponding parts of the congruent triangles are equal

$$\angle ABD = \angle ACD$$

In  $\triangle ABC$ , we have,

$$\angle ABD = \angle ACD$$

$\therefore AB = AC \dots$  Sides opposite to equal angles are equal

**29.** Here in  $\triangle ABC$   $AD$  and  $BE$  are medians.

Hence, in  $\triangle ABC$ , we have:

$$AC = AE + EC$$

But  $AE = EC \dots$  as  $E$  is midpoint of  $AC$

$$\therefore AC = 2EC \dots (1)$$

Now in  $\triangle BEC$ ,

$$DF \parallel BE$$

Also,  $EF = CF \dots$  by midpoint theorem, as  $D$  is the midpoint of  $BC$

But,

$$EC = EF + CF$$

$$\therefore EC = 2CF \dots (2)$$

From 1 and 2, we get,

$$AC = 4CF$$

$$\therefore CF = \frac{1}{4}AC.$$

**30.** (i)  $\angle ACD = 54^\circ$

$\angle ABD$  and  $\angle ACD$  are in the segment AD.

$\therefore \angle ACD = \angle ABD$  [Angles in the same segment of a circle]

$$\angle ACD = 54^\circ$$

(ii)  $\angle BAD = 43^\circ$

$\angle BAD$  and  $\angle BCD$  are in the segment BD.

$\therefore \angle BAD = \angle BCD$  [Angles in the same segment of a circle]

$$\angle BAD = 43^\circ$$

(iii)  $\angle BDA = 83^\circ$

In triangle ABD,

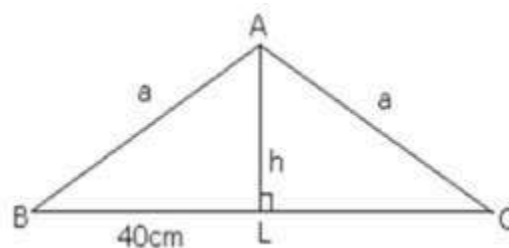
$\angle ABD + \angle BAD + \angle BDA = 180^\circ$  [Sum of angles of triangle]

$$\Rightarrow 54^\circ + 43^\circ + \angle BDA = 180^\circ$$

$$\Rightarrow 97^\circ + \angle BDA = 180^\circ$$

$$\Rightarrow \angle BDA = 83^\circ$$

**31.** Let us assume  $\triangle ABC$  be an isosceles triangle and let AL perpendicular BC



It is given that,



$$BC = 80 \text{ cm}$$

$$\text{Area of triangle ABC} = 360 \text{ cm}^2$$

We know that,

$$\text{Area of triangle} = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\frac{1}{2} \times BC \times AL = 360 \text{ cm}^2$$

$$\frac{1}{2} \times 80 \times h = 360 \text{ cm}^2$$

$$40 \times h = 360 \text{ cm}^2$$

$$h = \frac{360}{40}$$

$$= 9 \text{ cm}$$

Now,

$$BL = \frac{1}{2} (BC)$$

$$= \left(\frac{1}{2} \times 80\right)$$

$$= 40 \text{ cm}$$

$$a = \sqrt{BL^2 + AL^2}$$

$$= \sqrt{(40)^2 + (9)^2}$$

$$= \sqrt{1600 + 81}$$

$$= \sqrt{1681}$$

$$= 41 \text{ cm}$$

Therefore,

$$\text{Perimeter of the triangle} = (41 + 41 + 80) = 162 \text{ cm}$$



**32.** Given,

Dimensions of wall = 15m × 30cm × 4m = 1500 cm × 30 cm × 400 cm

Dimensions of each brick = 22 cm × 12.5 cm × 7.5 cm

Volume of wall = l × b × h = 1500 × 30 × 400 = 180000000 cm<sup>3</sup>

Area of mortar = 1/12 × volume of wall

$$= \frac{1}{12} \times 180000000 = 15000000 \text{ cm}^3$$

Hence,

Area occupied by bricks only = 180000000 - 15000000 = 165000000 cm<sup>3</sup>

Number of bricks required

$$= \frac{\text{volume for bricks only}}{\text{volume of one brick}} = \frac{165000000}{22 \times 12.5 \times 7.5} = 8000 \text{ bricks.}$$

**33.** Total number of Patients: 360

Number of Patients who are 30 Years or more but less than 40 years: 60

(This includes age groups between 30-40)

Number of Patients who are 50 Years or more but less than 70 years: 80

(This includes patients of age groups 50-60 and 60-70 therefore 50+30=80)

Number of Patients who are less than 10 years: 0 (No patients below 10 years)

Number of Patients who are 10 years or more: 360 (this include all age - groups admitted in the hospital)

$$\text{Probability } P(E) = \frac{\text{Number of favorable outcomes}}{\text{Total number of outcomes}}$$

(i). Let  $P(P_1)$  be probability of patients between age groups 30-40

$$P(P_1) = \frac{\text{Number of patients between age group 30-40}}{\text{Total number of patients}}$$

$$P(P_1) = \frac{60}{360} = \frac{1}{6}$$

(ii). Let  $P(P_2)$  be probability of patients between age groups 50-70

$$P(P_2) = \frac{\text{Number of patients between age groups 50-70}}{\text{Total number of patients}}$$

$$P(P_2) = \frac{80}{360} = \frac{2}{9}$$

(iii). Let  $P(P_3)$  be probability of patients who are less than 10 years

$$P(P_3) = \frac{\text{Number of patients who are less than 10 years}}{\text{Total number of patients}}$$

$$P(P_3) = \frac{0}{360} = 0$$

## Section – V

**34.** Given base  $QR = 6$  cm

$$\angle Q = 60^\circ$$

And  $PR - PQ = 2$  cms.

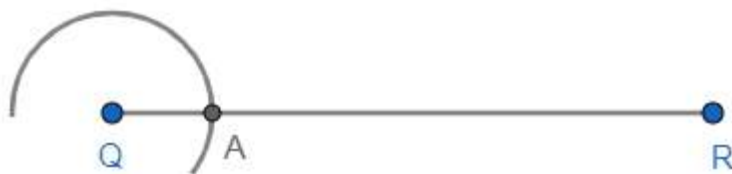
*Steps of construction:*

i. Draw a base line  $QR$  of 6 cms.



ii. Construct  $\angle Q = 60^\circ$ .

a. With  $Q$  as centre and with any radius, draw another arc cutting the line  $QR$  at  $A$ .

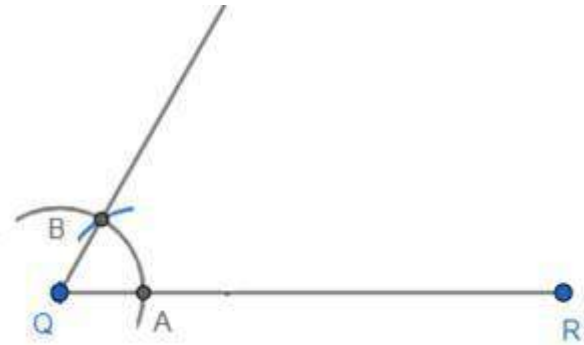


b. With  $A$  as centre and with the same radius, draw an arc cutting the first arc (drawn in step a) at point  $B$ .





c. Now join the ray QB which forms an angle of  $60^\circ$  with the line QR.

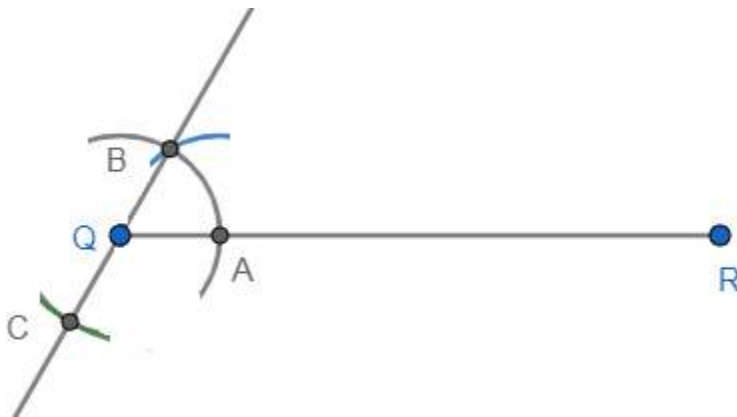


As,  $PR - PQ = 2$

$PR > PQ$

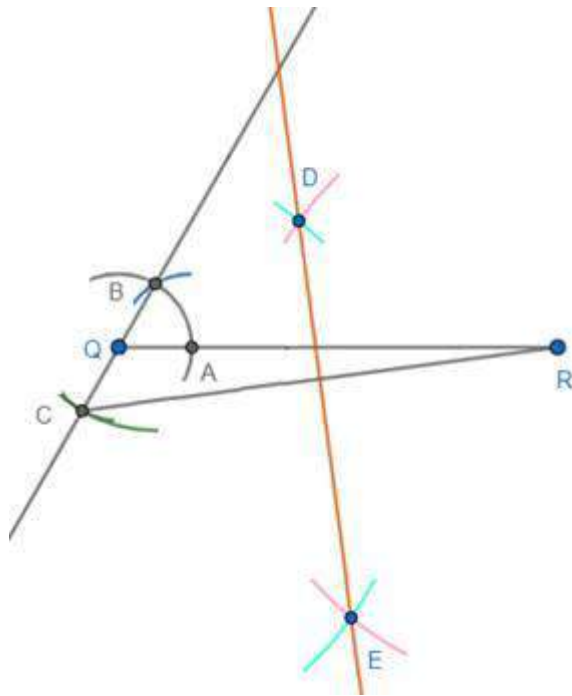
So the ray QB will be below QR

iii. Extend the ray QB below QR. With Q as centre draw an arc with length 2 cms ( = PR- PQ given), such that it intersects ray QB at C below QR.

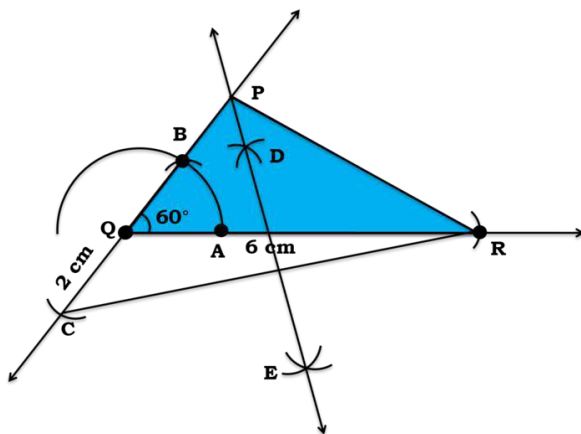


iv. Join CR and draw a perpendicular bisector for CR.

- a. By drawing arcs on both sides of the line CR, with C and R as centers and with same lengths which is more than half length of CR. These arcs intersect at D and E on either side of line CR.



v. The perpendicular bisector for CR will intersect the ray QB at point P. Join PR.



Thus, the formed triangle PQR is the required triangle.

**35.** External height ( $l$ ) of book self = 85 cm

External breadth ( $b$ ) of book self = 25 cm

External height ( $h$ ) of book self = 110 cm

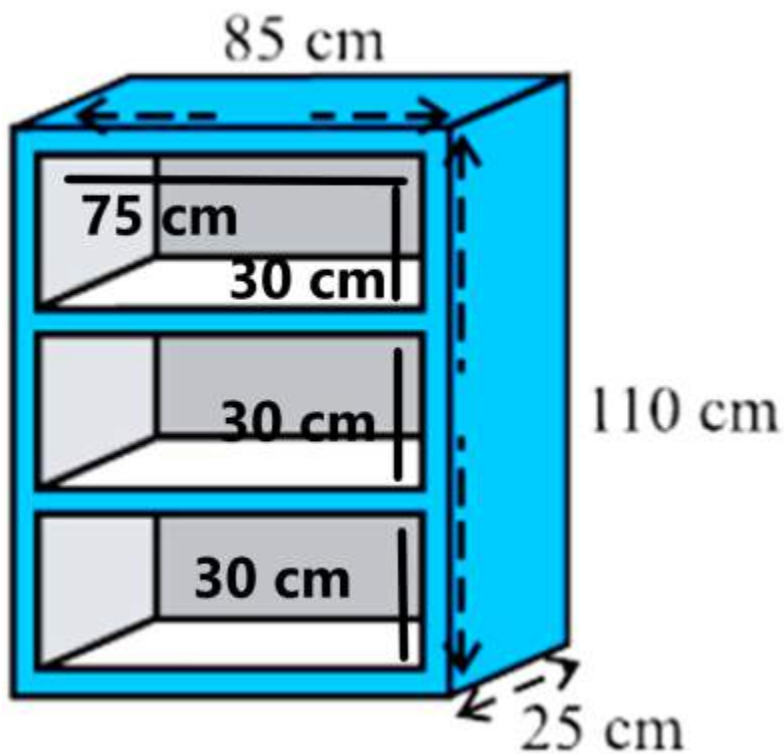
The external surface area of the shelf while leaving out the front face of the shelf =  $lh + 2(lb + bh)$

$$= [85 \times 110 + 2(85 \times 25 + 25 \times 110)]$$

$$= (9350 + 9750)$$



$$= 19100 \text{ cm}^2$$



we know each stripe on the front surface is also to be polished. which is 5 cm stretch.

$$\text{Area of front face} = [85 \times 110 - 75 \times 100 + 2 (75 \times 5)]$$

$$= 1850 + 750$$

$$= 2600 \text{ cm}^2$$

$$\text{Area to be polished} = (19100 + 2600) = 21700 \text{ cm}^2$$

$$\text{Cost of polishing } 1 \text{ cm}^2 \text{ area} = \text{Rs } 0.20$$

$$\text{Cost of polishing } 21700 \text{ cm}^2 \text{ area} \text{ Rs } (21700 \times 0.20) = \text{Rs } 4340$$

It can be observed that length (l), breadth (b), and height (h) of each row of the bookshelf is 75 cm, 20 cm, and 30 cm respectively

$$\text{Area to be painted in 1 row} = 2 (l + h) b + lh$$

$$= [2 (75 + 30) \times 20 + 75 \times 30]$$

$$= (4200 + 2250)$$

$$= 6450 \text{ cm}^2$$

$$\text{Area to be painted in 3 rows} = (3 \times 6450)$$

$$= 19350 \text{ cm}^2$$

Cost of painting 1 cm<sup>2</sup> area = Rs 0.10

Cost of painting 19350 cm<sup>2</sup> area = Rs (19350 × 0.1)

= Rs 1935

Total expense required for polishing and painting = Rs (4340 + 1935)

**= Rs 6275**

**36.** The parts of the questions are solved below:

(i) The data is represented in a discontinuous class interval. So, at first we will make it continuous.

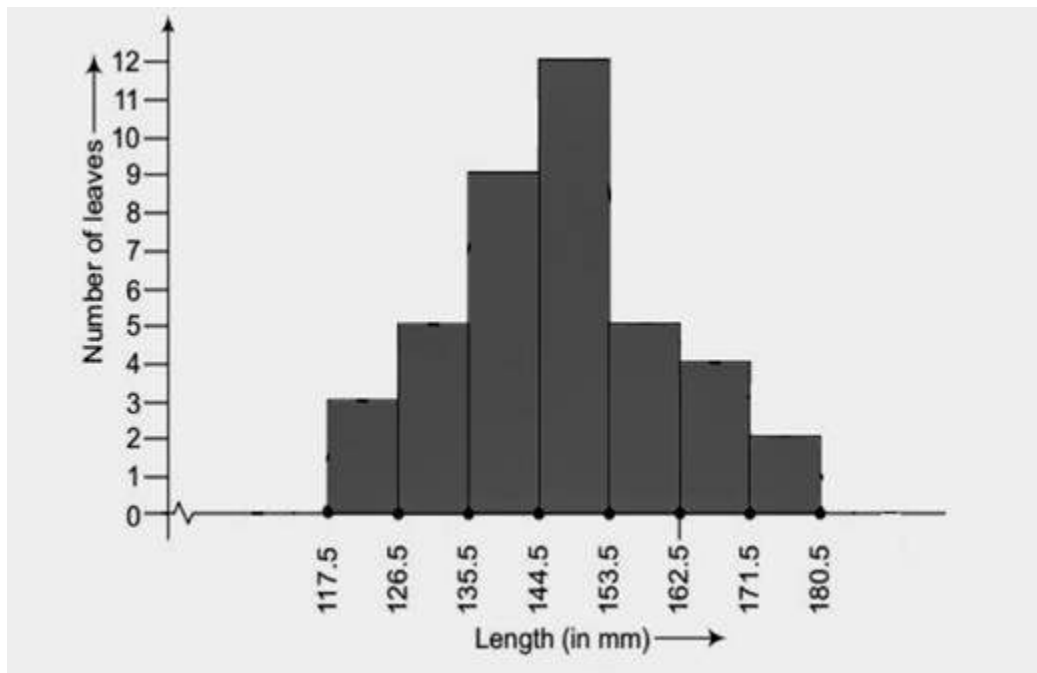
The difference is 1.

So, we subtract 0.5 from the lower limit and add 0.5 to the upper limit.

S.No.	Length (in mm)	Number of Leaves
1.	117.5-126.5	3
2.	126.5-135.5	5
3.	135.5-144.5	9
4.	144.5-153.5	12
5.	153.5-162.5	5
6.	162.5-171.5	4
7.	171.5-180.5	2



Now, the above information is represented by the histogram below:



(ii) No, it is incorrect to conclude that the maximum number of leaves are lying between length of 144.5 – 153.5

Explanation: Maximum length of leaf lies between 144.5 - 153.5, it is not necessarily 153 mm. It can be any value between the range.

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